

Constraint-based reachability: test input generation for C code

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Outline

Introduction

Constraint-based program exploration

Euclide: An implementation for C code

Conclusions & Perspectives

// Constraint-based reachability (CBR)

For a given program P and location loc in P , constraint-based reachability (CBR) is the process of determining : 1) if loc is reachable and 2) inputs values for P , in order to reach loc by using constraint solving techniques (CSP, LP, SAT, SMT, ...)

Reachability problems in infinite-state systems are undecidable in general!


Introduced 20 years ago by Offut and DeMillo in
(Constraint-based automatic test data generation IEEE TSE 1991)

Developed in the context of **software testing**
(e.g., symbolic evaluation, mutation testing)

Lots of Research works and tools!

Solving CBR problems involves constraint solving

Even when adding bounds,
hard combinatorial problem

```
f(int x1, int x2, int x3) {  
    if(x1 == x2 && x2 == x3)  
        if(x3 == x1 * x2) ... } 
```

Using Random Testing,
Prob{ reach k } = 2 over $2^{32} \times 2^{32} \times 2^{32} = 2^{-95} = \mathbf{0.00000...1}$.

Constraint solving techniques are required!

- ✓ Loops (i.e., infinite-state systems) and infeasible paths
- ✓ Pointers, dynamic structures, higher-order computations (virtual calls)
- ✓ Floating-point computations, modular computations

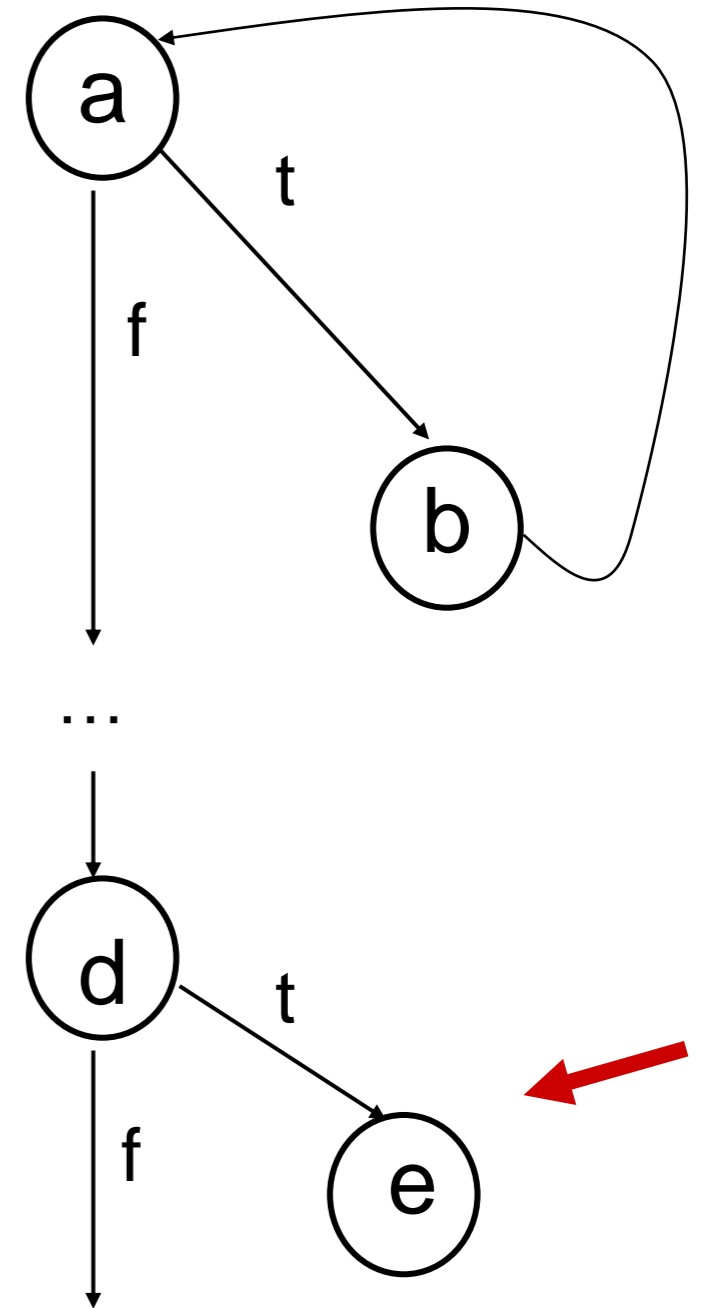
Our contribution:
Constraint-based program exploration

A CBR problem

```
f( int i, ... )  
{  
a.   j = 100;  
    while( i > 1)  
b.     { j++ ; i-- ; }  
  
    ...  
d.   if( j > 500)  
e.     ...
```



value of i to reach e ?



Path-oriented exploration

```
f( int i, ... )  
{
```

```
a.   j = 100;  
    while( i > 1)  
b.     { j++ ; i-- ; }
```

```
...
```

```
d.   if( j > 500)
```

```
e.     ...
```

1. Path selection

e.g., (a-b)¹⁴-...-d-e

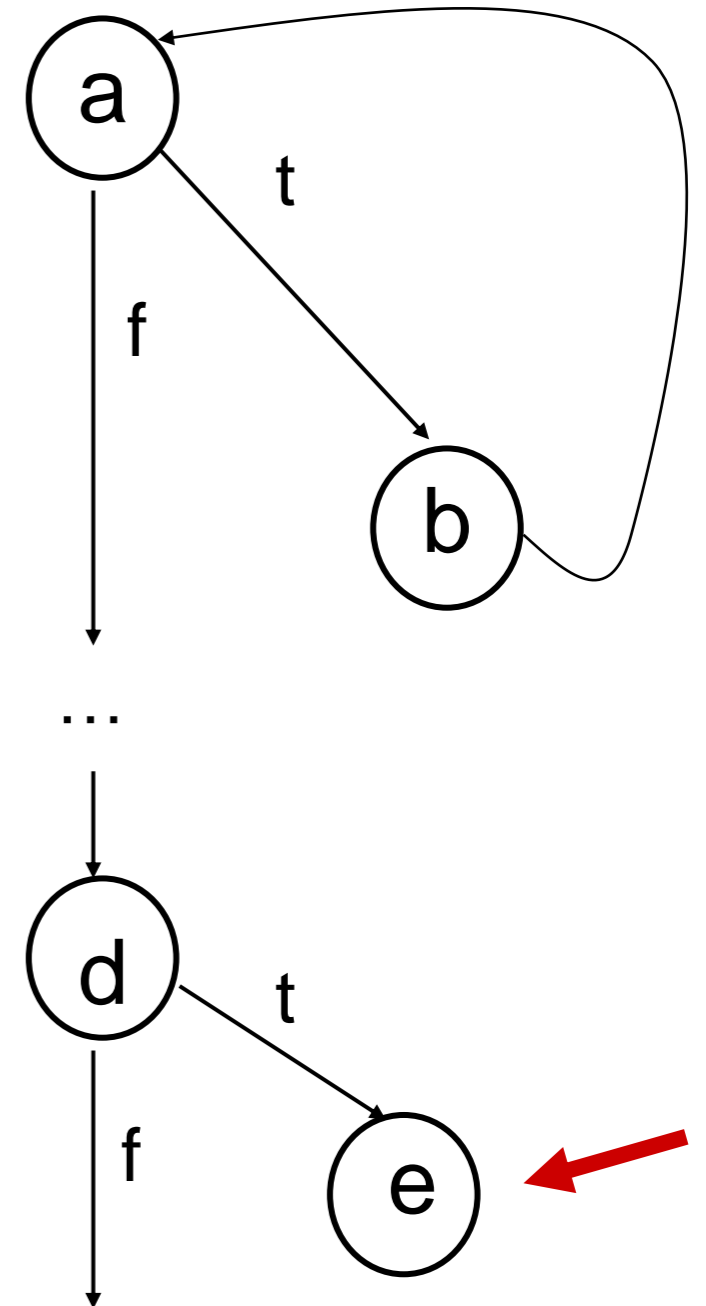
2. Path condition generation (via symbolic exec.)

$j_1=100, i_1>1, j_2=j_1+1, i_2=i_1-1, i_2>1, \dots, j_{15}>500$

3. Path condition solving

unsatisfiable → FAIL

Backtrack!



Even without loops, #paths is exponential with #decisions

Constraint-based program exploration

```
f( int i, ... )  
{
```

```
a.   j = 100;  
    while( i > 1)  
b.   { j++ ; i-- ; }
```

```
...
```

```
d.   if( j > 500)
```

```
e.   ...
```

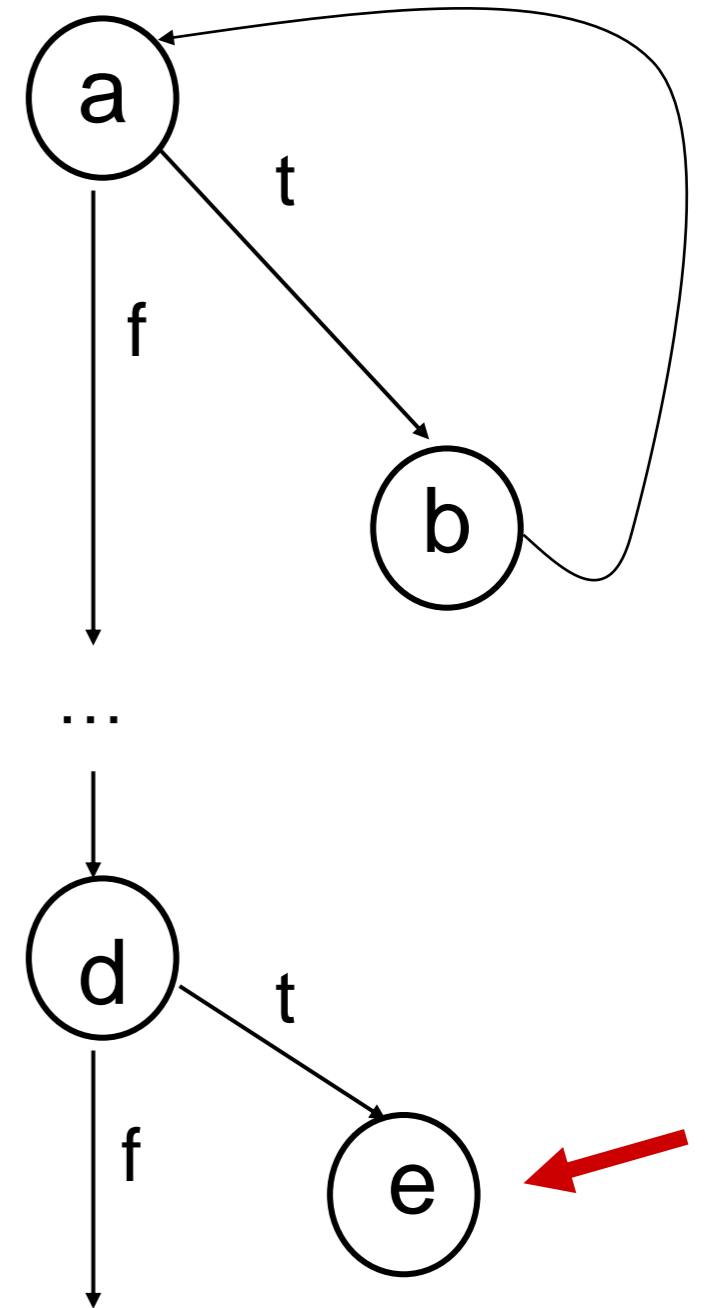
1. Constraint model generation

2. Control dependencies generation;

$j_1=100, i_3 \leq 1, j_3 > 500$

3. Constraint model solving

$j_1 \neq j_3$ entailed \rightarrow unroll the loop 400 times $\rightarrow i_1$ in $401 .. 2^{31}-1$



No backtrack !

Constraint-based program exploration

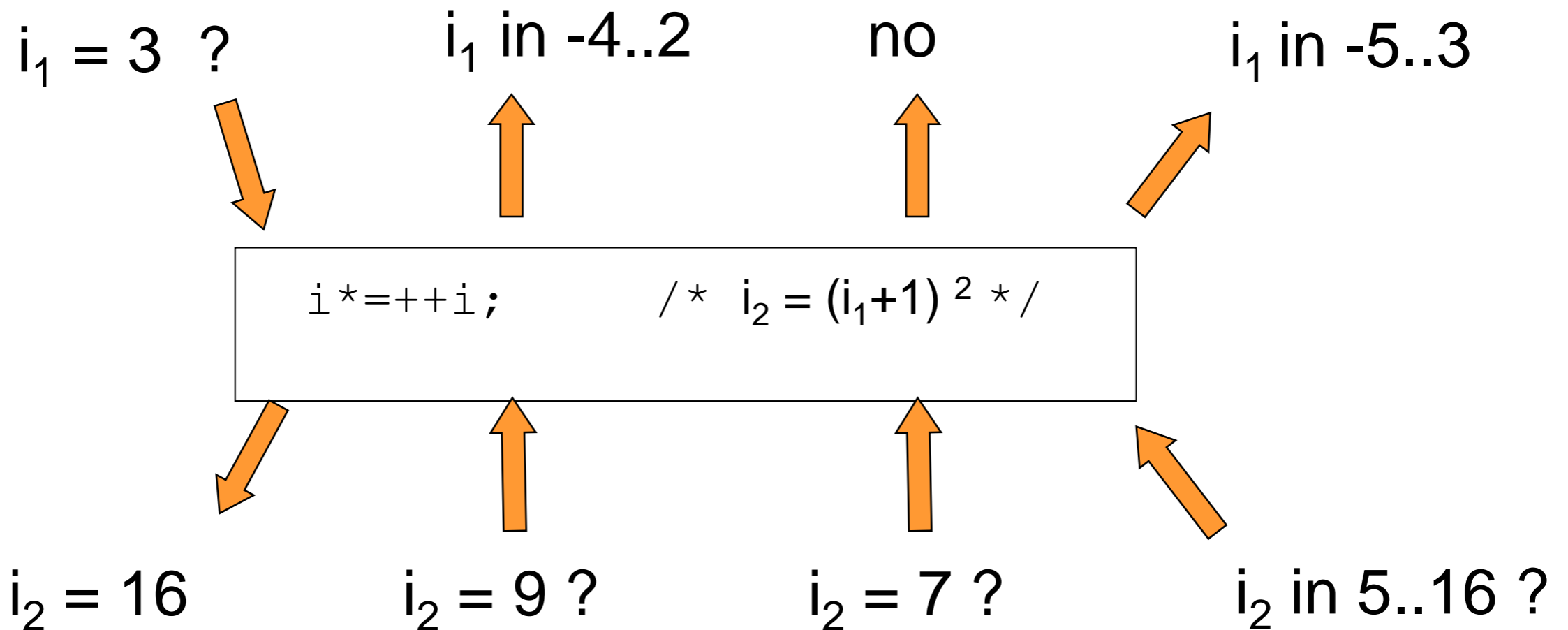
- Based on a constraint model of the whole program (Constraint Programming)
- Constraint reasoning over control structures → meta-constraints
- Requires to build **dedicated constraint solvers**:
 - * filtering techniques, propagation queue management with priorities
 - * specific meta-constraints for handling pointers and memory updates, floating-point computations, function calls, ...
 - * structure-aware labelling heuristics

Assignment as Constraint

Viewing an assignment as a relation requires to normalize expressions and rename variables (through single assignment languages, e.g. SSA)

$$i^{*} = ++i ; \quad \longrightarrow \quad i_2 = (i_1 + 1)^2$$

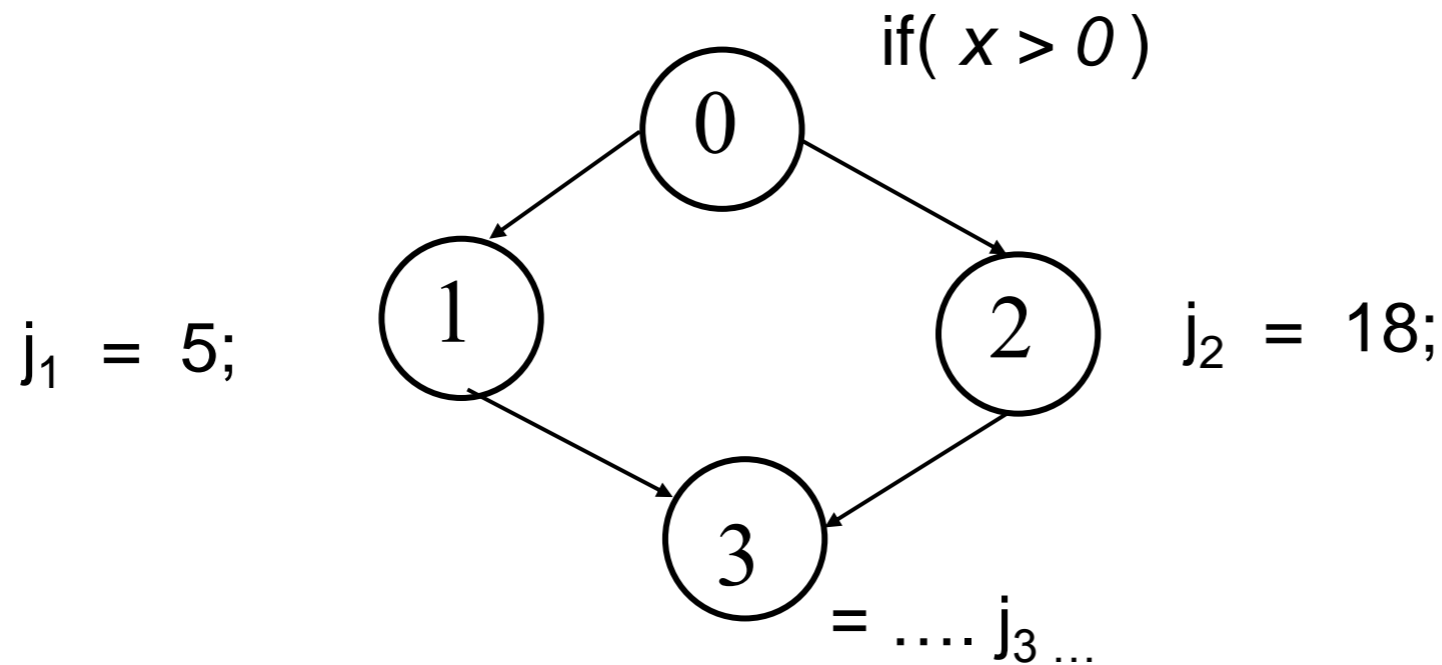
Using classical filtering techniques over finite domains:



Statements as constraints

- ✓ Type declaration: `signed long x;` $\rightarrow x \text{ in } -2^{31}..2^{31}-1$
- ✓ Assignments: `i*=++i ;` $\rightarrow i_2 = (i_1+1)^2$
- ✓ Memory and array accesses and updates:
`v=A[i] (or p=Mem[&p])` \rightarrow variations of element/3
- ✓ Control structures: dedicated meta-constraints
(interface, awakening conditions and filtering algorithms)
 - Conditionnals (SSA) `if D then C1; else C2` \rightarrow ite/6
 - Loops (SSA) `while D do C` \rightarrow w/5

Conditional as meta-constraint: ite/6

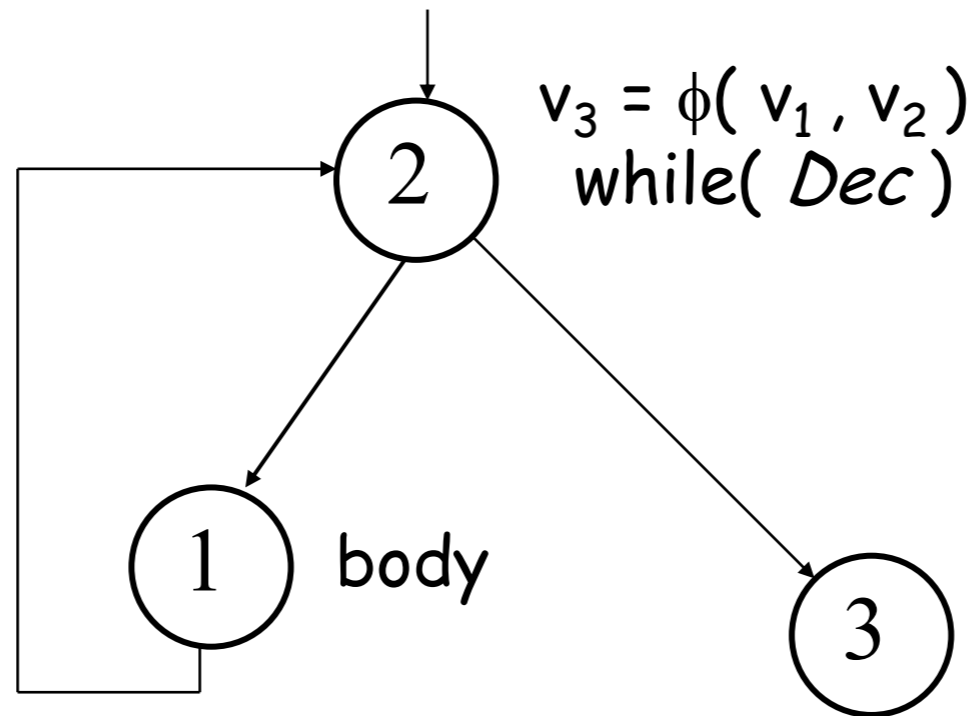


$\text{ite}(x > 0, j_1, j_2, j_3, j_1 = 5, j_2 = 18)$ iff

- ◆ $x > 0 \rightarrow j_1 = 5 \wedge j_3 = j_1$
- ◆ $\neg(x > 0) \rightarrow j_2 = 18 \wedge j_3 = j_2$
- ◆ $\neg(x > 0 \wedge j_1 = 5 \wedge j_3 = j_1) \rightarrow \neg(x > 0) \wedge j_2 = 18 \wedge j_3 = j_2$
- ◆ $\neg(\neg(x > 0) \wedge j_3 = j_2) \rightarrow x > 0 \wedge j_1 = 5 \wedge j_3 = j_1$
- ◆ $\text{Join}(x > 0 \wedge j_1 = 5 \wedge j_3 = j_1, \neg(x > 0) \wedge j_2 = 18 \wedge j_3 = j_2)$

Implemented as a regular constraint
(interface, awakening conditions, filtering algo.)

Loop as meta-constraint: w/5



$w(\text{Dec}, V_1, V_2, V_3, \text{body})$ iff

- ◆ $\text{Dec}_{V_3 \leftarrow V_1} \rightarrow \text{body}_{V_3 \leftarrow V_1} \wedge w(\text{Dec}, v_2, v_{\text{new}}, v_3, \text{body}_{V_2 \leftarrow V_{\text{new}}})$
- ◆ $\neg \text{Dec}_{V_3 \leftarrow V_1} \rightarrow v_3 = v_1$
- ◆ $\neg(\text{Dec}_{V_3 \leftarrow V_1} \wedge \text{body}_{V_3 \leftarrow V_1}) \rightarrow \neg \text{Dec}_{V_3 \leftarrow V_1} \wedge v_3 = v_1$
- ◆ $\neg(\neg \text{Dec}_{V_3 \leftarrow V_1} \wedge v_3 = v_1) \rightarrow \text{Dec}_{V_3 \leftarrow V_1} \wedge \text{body}_{V_3 \leftarrow V_1} \wedge w(\text{Dec}, v_2, v_{\text{new}}, v_3, \text{body}_{V_2 \leftarrow V_{\text{new}}})$
- ◆ $\text{join}(\text{Dec}_{V_3 \leftarrow V_1} \wedge \text{body}_{V_3 \leftarrow V_1} \wedge w(\text{Dec}, v_2, v_{\text{new}}, v_3, \text{body}_{V_2 \leftarrow V_{\text{new}}}), \neg \text{Dec}_{V_3 \leftarrow V_1} \wedge v_3 = v_1)$

```
f ( int i ) {
  j = 100;
  while ( i > 1 )
    { j++ ; i-- ; }
  ...
  if ( j > 500 )
    ...
```

w(Dec, V₁, V₂, V₃, body) :-

- ◆ Dec_{V₃←V₁} → body_{V₃←V₁} ∧ w(Dec, v₂, v_{new}, v₃, body_{V₂←V_{new}})
- ◆ ¬Dec_{V₃←V₁} → v₃=v₁
- ◆ ¬(Dec_{V₃←V₁} ∧ body_{V₃←V₁}) → ¬Dec_{V₃←V₁} ∧ v₃=v₁
- ◆ ¬(¬Dec_{V₃←V₁} ∧ v₃=v₁) →
Dec_{V₃←V₁} ∧ body_{V₃←V₁} ∧ w(Dec, v₂, v_{new}, v₃, body_{V₂←V_{new}})
- ◆ join(Dec_{V₃←V₁} ∧ body_{V₃←V₁} ∧ w(Dec, v₂, v_{new}, v₃, body_{V₂←V_{new}},
¬Dec_{V₃←V₁} ∧ v₃=v₁)

i = 23, j₁ = 100 ?

no

i in 401..2³¹-1

w(i₃ > 1, (i, j₁), (i₂, j₂), (i₃, j₃), j₂ = j₃ + 1 ∧ i₂ = i₃ - 1)

i₃ = 1, j₃ = 122

i₃ = 10 ?

j₁ = 100,
j₃ > 500 ?

Features of constraint-based exploration

- ✓ Special meta-constraints implementation for ite and w

By construction, w is unfolded only when necessary

but **w may NOT terminate !**

→ only a **semi-correct** test input generation procedure

- ✓ Join is implemented using **Abstract Interpretation** operators (e.g., Interval and Polyhedral union, widening in **Euclide**, Difference constraints in **Gatel**, Congruences in **JSolver**)
- ✓ Special propagators based on linear-based relaxations
Using **Linear Programming over rationals** (i.e., Q_polyhedra)

EUCLIDE: An implementation for C code

EUCLIDE

Euclide (C:/Users/gotlieb/gotlieb/RECHERCHE/EUCLIDE_V0/examples/ardeta03.c)

File Edit Tools Zoom Help

```
void P_rad_eta()  
{  
    MEM_PBMORDR = PBMORDR;  
    PBMORDR = 0x0;  
    FM_PBMORDR = 0x0;  
  
    if (!MSTRDR)  
    {  
        TPMSTRDR = 94;  
        TPCODRDR = 194;  
        TPIEMRDR = 1875;  
        MERDR = 0;  
    }  
    else  
    {  
        if (TPCODRDR != 194)  
        {  
            if (TPCODRDR <= 0)  
            {  
                trait2_eta();  
            }  
            else  
            {  
                if (TPCODRDR <= (194 - 13))  
                {  
                    if (!DIALRDR)  
                    {  
                        trait3_eta();  
                    }  
                    else  
                    {  
                        local_merdr3g = TP_RDR_7R.merdr3g  
                        if ((local_merdr3g & 0x0001)==0x0001)  
                        {  
                            trait1_eta();  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

Legend:

- I/O Node (White circle)
- Decision Node (Blue circle)
- Code Node (Grey circle)
- Goto/Label Node (Red circle)
- Cte/Brk Node (Green circle)
- Return Node (Green circle)

Diagram: Control flow graph for P_rad_eta. The graph shows a sequence of nodes connected by arrows. Red arrows indicate the execution path, starting from the entry node, through the first if-else block, then through the nested if-else blocks, and finally reaching the return node. The graph is titled "P_rad_eta".

Symmetric program

Automatic Test Data Generation

Components	Test Data
File : C:/Users/gotlieb/gotlieb/RECHERCHE/EUCLIDE_V0/examples/ardeta03.cpp	TPCODRDR = 91
Subroutine : P_rad_eta	merdr3g*TP_RDR_7R = 65534
Target node : 21	local_merdr3g = 32767
Formal parameters : []	merdr0g*TP_RDR_7R = 32767
Global used : [id(TPCODRDR,514,[type(unsigned_short_int,2)],rf(no)), .point([id(merdr3g,79,[type(unsigned_short_int,2)],rf(no)),id(TP_RDR_7R,507,[type(unsigned_short_int,2)],rf(no)),id(TP_RDR_7R,507,[type(unsigned_short_int,2)],rf(no))],rf(no)),id(TP_RDR_7R,507,[type(unsigned_short_int,2)],rf(no))],rf(no))]	local_merdr0g = 32767
	TPIEMRDR = 0
	MEM_PBMORDR = 32767
	DIALRDR = 32768
	PBMORDR = 0
	MSTRDR = 32768
	TPMSTRDR = 0
	MERDR = 32767

Confirm
Keep & Close
Close

Conclusions & Perspectives

Conclusions

- Constraint Programming is a convenient and efficient tool for reasoning over imperative programs, as it enables:
 - constraint design and constraint-based program exploration ;
 - **relational modelling** for reachability problems;
 - implementations are available! (e.g., EUCLIDE, PathCrawler)
-
- But **unsatisfiability (UNSAT) detection** has to be improved (e.g., by combining techniques from SMT-solving)
 - But **constraint solvers** are so tuned and optimized, that they cannot be easily showed bug-free, and blindly trusted!

Perspectives

- Constraint solving over floating-point computations
(Bagnara Carlier Gori Gotlieb, ICST'2013)

Collaboration with U.of Parma, Italy – PhD Thesis

- Formal certification of a consistency filtering constraint solver
(Carlier Dubois Gotlieb, FM'12)

Collaboration with INRIA, France – AURORA CertiSkatt Project

Thank you!